

# Data assimilation experiment on SO<sub>2</sub> initial conditions in the Pearl River Delta

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## Introduction

As the air pollution problem become more and more severe, many air quality models were developed and applied to research and forecast operation. However there are many uncertainties in the model, which affect the forecast result. Data assimilation is a state-of-the-art approach to reduce the uncertainties in input data, such as initial conditions or boundary conditions, by using observations. It can combine both advantages of model results and observations to improve the prediction.

In order to provide a more precise initial condition of SO<sub>2</sub> in the Pearl River Delta (PRD) region, data assimilation methods were introduced to the WRF-CMAQ model. Sensitivity experiments were carried out to exam the number of assimilation site and correlation scale. The comparative experiment on the optimal effect of different assimilation methods were conducted.

## Methodology

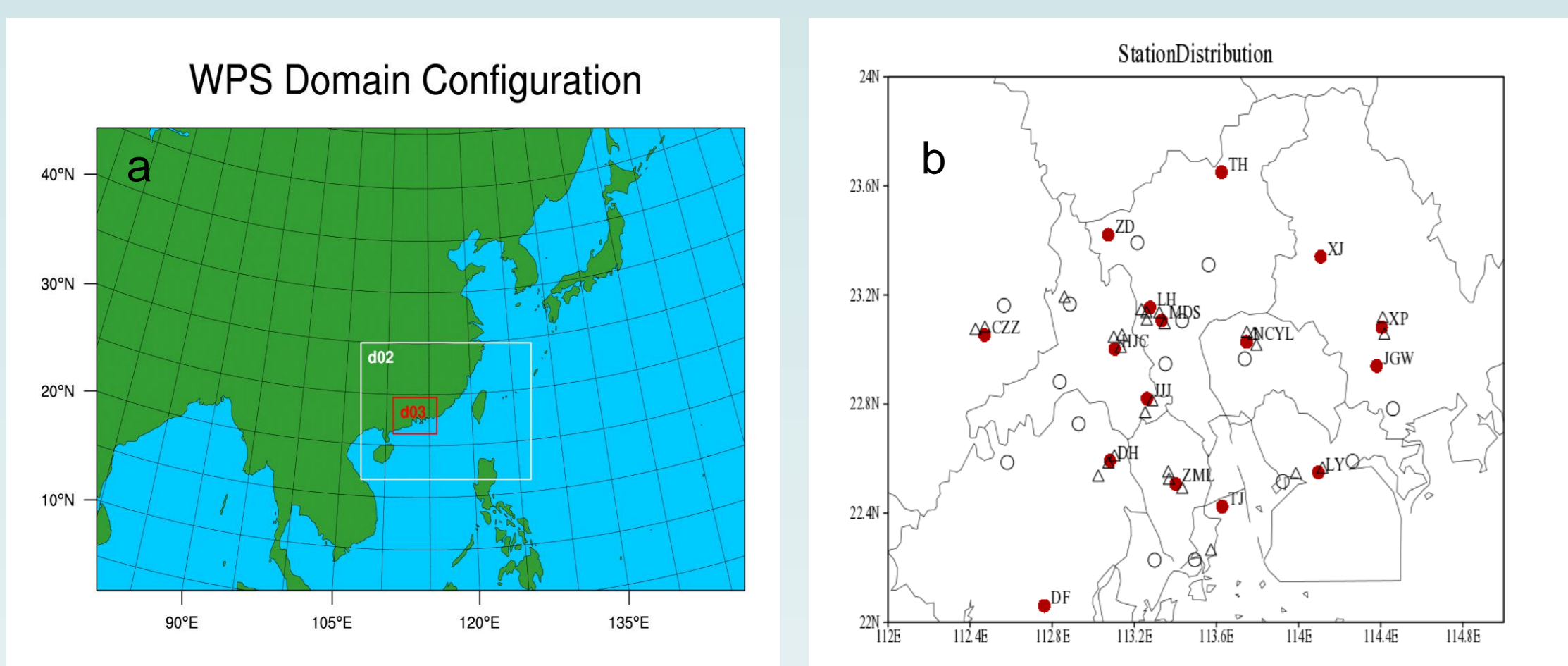


Fig.1(a) Nesting domain setting of the WRF-CMAQ model, domain 01(27x27km), domain 02 (9x9km) and domain 03 (3x3km); (b) Domain 03 shows the distribution of observation sites in the PRD region where we have the assimilation experiment.

The method used here is the Optimal Interpolation method (OI) and the Ensemble Square Root Filter method (EnSRF). The formula as follows:

$$\begin{aligned}
 & \text{OI} & \text{EnSRF} \\
 & x^a = x^b + K(y^o - Hx^b) & \bar{x}^a = \bar{x}^b + K(\bar{y}^o - H\bar{x}^b) \\
 & K = B^b H^T (HB^b H^T + R)^{-1} & x^a = x^b - \tilde{K} H x^b \\
 & & K = B^b H^T (HB^b H^T + R)^{-1} \\
 & & \tilde{K} = \alpha K, \quad B^b = \frac{x^b x^{bT}}{N-1} \\
 & & \alpha = \left( 1 + \frac{R}{\sqrt{HB^b H^T + R}} \right)^{-1} \\
 & & x^a = \bar{x}^a + x^a
 \end{aligned}$$

$x^a$ : analysis field,  $x^b$  background field,  
 $x^{12}$  and  $x^{24}$ : 12h and 24h forecast fields  
 $y^o$ : observation field, H: operator,  $B^b$ : background error covariance  
R: observation error covariance, N: number of ensemble, here is 30  
Superscript : T and -1, transpose and inversion of Matrix  
- and 'average and bias of ensemble

## Results and Discussion

### Model Evaluation

Table 1 Statistical comparison of simulated and observed meteorological parameters

Location	Parameter	Value	Value	Value
Guangzhou	T		RH	WS
	Mean Bias (MB)	0.23	-2.96	1.70
	Mean Absolute Gross Error (MAGE)	1.87	12.94	1.84
	Normal Mean Bias (NMB)	3%	3%	70%
	Normal Mean Error (NME)	0.18	0.23	0.74
	Index of Agreement (IOA)	0.94	0.82	0.67
Correlation Coefficient (CORR)		0.88	0.72	0.70

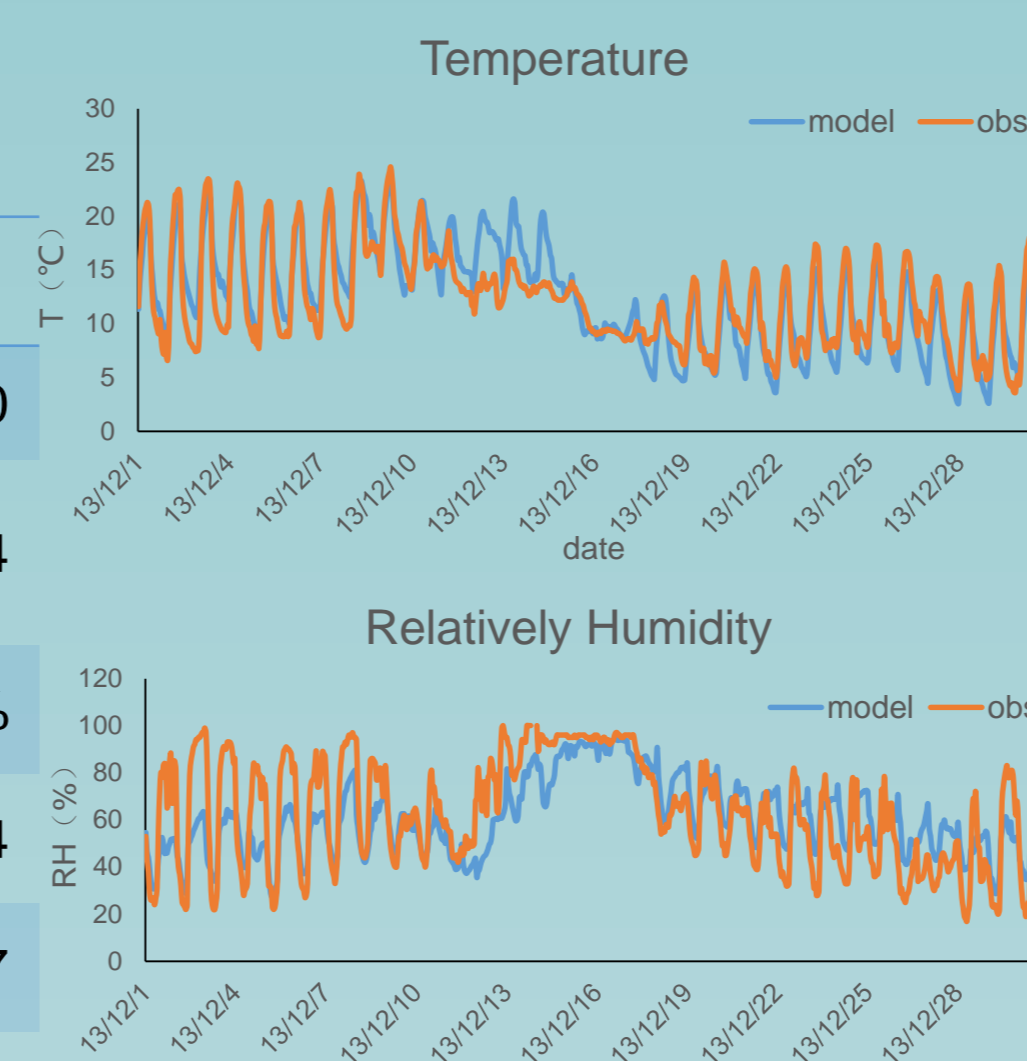


Fig. 2 Temporal variations of temperature and relatively humidity

Table 2 Statistical analyses of modelling performance on daily mean SO<sub>2</sub>

Parameter	SO <sub>2</sub>	ave	max	min
MB		9.42	41.87	-34
MAGE		17.79	41.87	5.14
NMB		61.11%	389.00%	-50.00%
NME		84.13%	389%	17%
RMSE		20.93	45.96	7.15
CORR		0.75	0.93	0.34

Generally, diurnal variations of temperature and relatively humidity are well captured by model, the simulation of wind speed and SO<sub>2</sub> are relatively high.

### Background Analyses

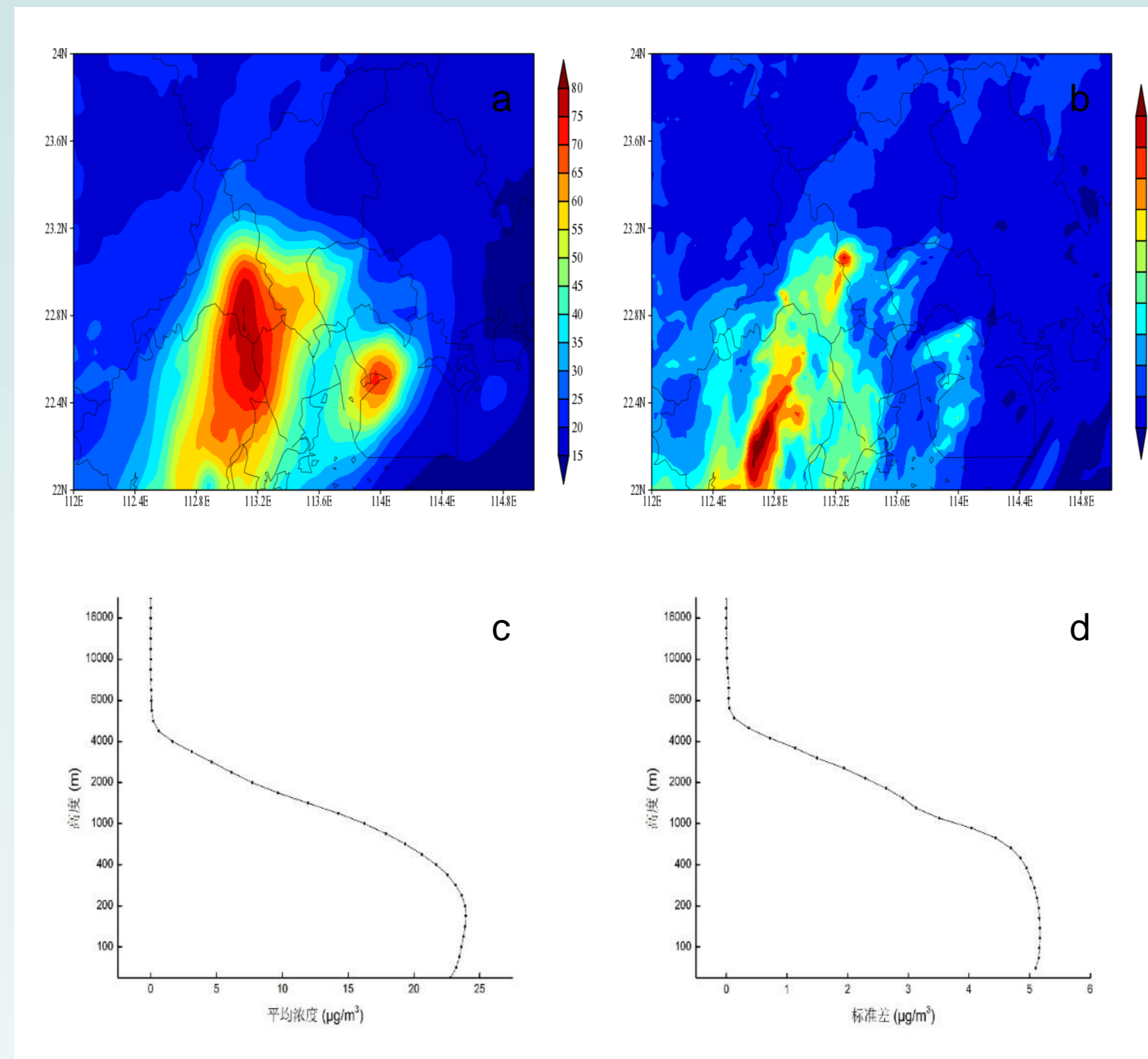


Fig.3(a) Distribution of the monthly average concentration of SO<sub>2</sub> at the first model level; (b) Distribution of the standard error of SO<sub>2</sub> at the first model level; (c) Vertical profile of monthly average concentration of SO<sub>2</sub>; (d) Vertical profile of monthly average concentration of SO<sub>2</sub>.

Horizontally, the high value region of error didn't fit the concentration well. Locate in southwest region;

Vertically, the variation of error and concentration are similar. Constant below 400m, decrease above 400m.

### Number of assimilation site

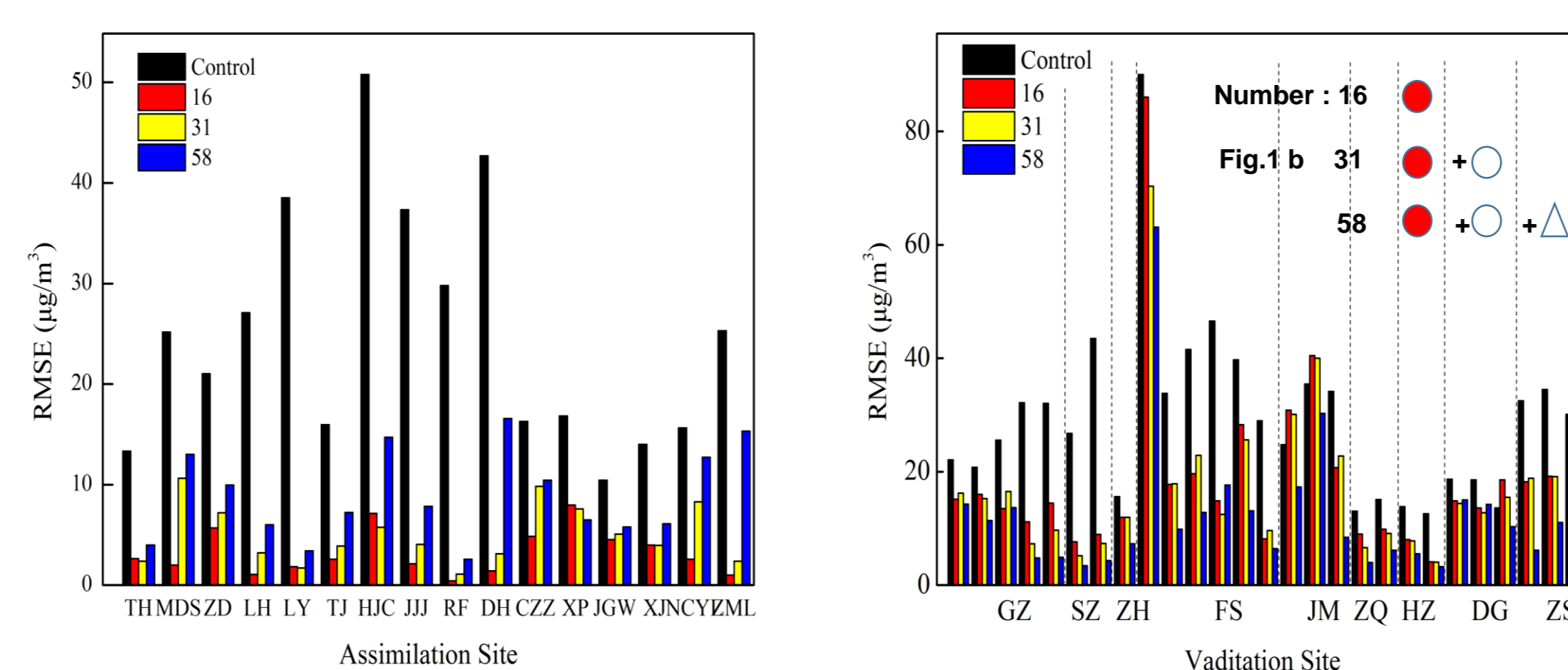


Fig.4 Comparisons of RMSE with assimilating different numbers of observations by OI

Increasing the number is beneficial for broadening the coverage of site. But the optimal effect of the assimilation site decrease with the number of observations statistically.

### Correlation Scale

Table 3 Statistics of the result with different correlation scales of different methods

Sites	Control	Method	10km	20km	30km	40km	50km	60km	80km	100km
			Assimilation	MAGE	21.39	OI: 2.79, 4.59, 7.07, 8.84, 10.65, 12.11, 13.62, 14.68	EnSRF: 1.68, 2.55, 3.40, 4.16, 4.87, 5.51, 6.31, 6.81	RMSE	27.08	OI: 4.42, 6.84, 10.42, 12.83, 14.98, 16.69, 18.43, 19.68
Validation	MAGE	23.91	OI: 12.95, 13.05, 13.18, 13.19, 12.99, 13.30, 14.14, 14.79	EnSRF: 12.00, 12.35, 12.95, 13.12, 13.37, 13.58, 14.16, 14.57	RMSE	29.48	OI: 17.81, 17.60, 17.82, 18.20, 18.42, 18.94, 20.02, 20.75	EnSRF: 16.75, 17.08, 17.70, 17.84, 18.29, 18.51, 19.41, 19.99		

Correlation scale decides the influence radius of the observation. The error of the analysis field increases with the correlation scale. Setting 20km will be more reasonable.

### Different Methods

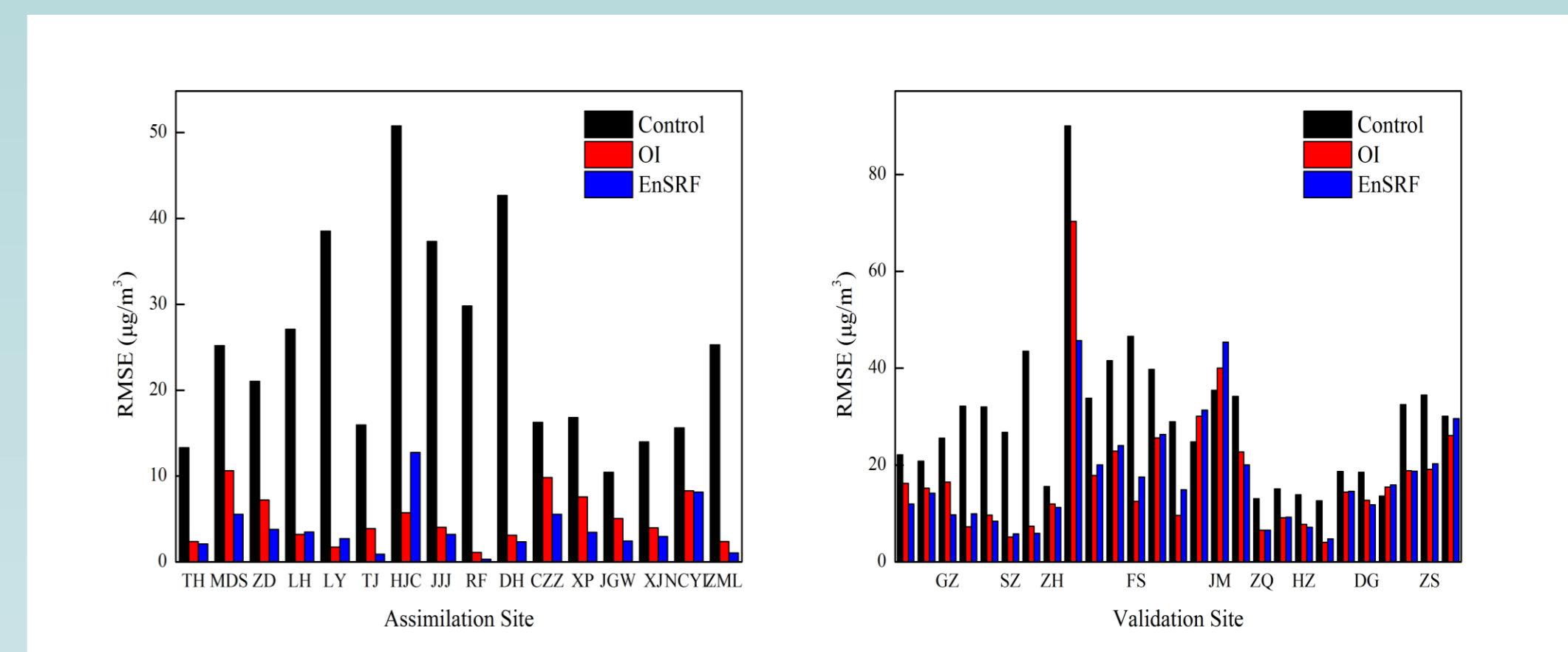


Fig.5 Comparisons of RMSE with and without assimilation using different methods (Assimilation sites 31, Correlation scale 20km)

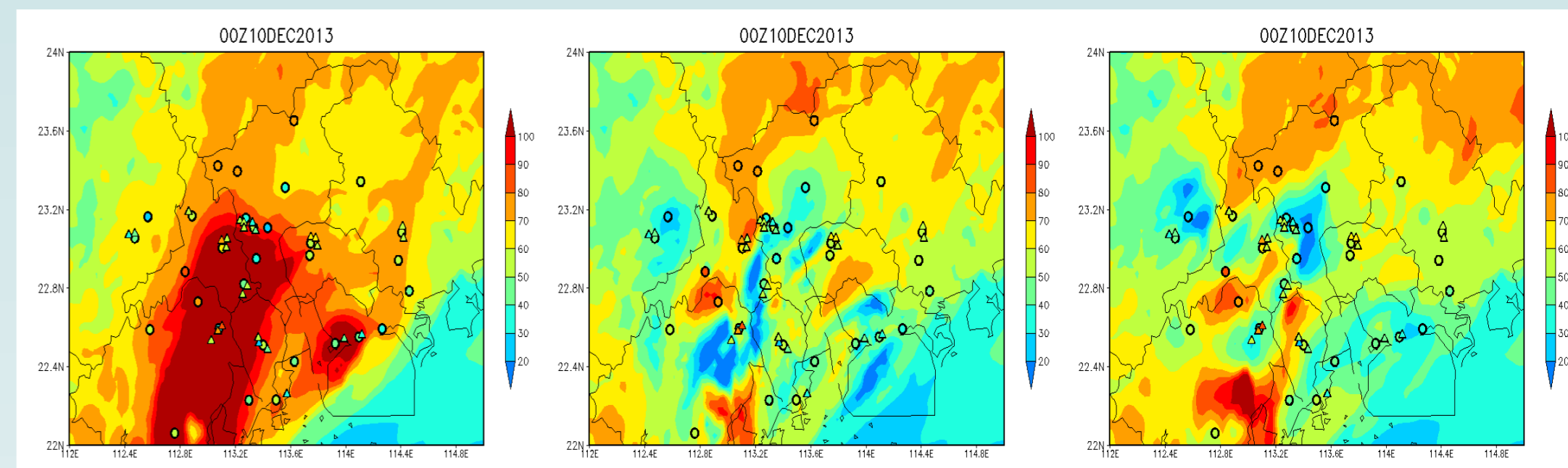


Fig.6 Distribution pattern of SO<sub>2</sub> concentration

As a whole, both assimilation methods reduced the error, the optimal result of EnSRF is better than OI;

Both methods adjusted the distribution pattern of SO<sub>2</sub> and make it more closed to the observation filed.

## Conclusion

The simulation of temperature and relative humidity were well, but higher for simulation of the wind speed and SO<sub>2</sub> is relatively high by WRF-CMAQ.

The high values of the background error was mainly located in southwest region in horizontal direction. It was nearly constant below 400m and decreased with height above 400m.

The sensitivity test showed that the optimal horizontal scale was 20km. With the number of the assimilation site increasing, the optimization of the assimilation site had a declining trend.

Under the same conditions, the optimization of EnSRF method is better than that of OI method. Both methods can provide an analysis field closer to reality.

## Contact Information

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